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Spatially-Varying Calibration of Along-Track Monopulse Synthetic Aperture Radar Imagery for Ground Moving Target Indication and Tracking

Uttam Majumder, Mehrdad Soumekh, Michael Minardi, John Kirk



Air Force Research Laboratory (AFRL/RYAS)

Soumekh Consulting









- 1. Objectives
- 2. Multiple Moving Targets Detection
- 3. Multiple Moving Targets Association and Tracking
- 4. Ground Plane Geolocation
- 5. Summary







- 1. Detect multiple moving targets in a heavy clutter (urban) environment using a singlepass with one or more along-track receivers and/or multiple-pass SAR
- 2. Associate detections in subaperture SAR imagery to identify the radial-range and Doppler tracks of each target
- **3. Geolocate** each detected and tracked moving target using its subaperture radialrange and Doppler data with or without information on network of roads



- SAR-MTI is constructed using a 2D adaptive change detection algorithm
- We have tested three types of databases (options) to form *Reference* and *Test* images.
- The option that is presented is this paper is:
 - Subaperture monostatic and along-track bistatic (DPCA) monopulse SAR data from a single pass (coherent change detection)





Why **subaperture**-based processing?

- For an IR or visible camera, a moving target appears: a) slightly blurred but still detectable via change detection in an image sequence; & b) around its true spatial coordinates (on camera's focal plane)
- In a full-aperture (-resolution) SAR image: a) to say a moving vehicle signature appears blurred is an understatement; & b) the mover signature would be Doppler-shifted
- In a subaperture SAR image, a mover would be more localized for detection purposes though still Doppler-shifted



- 2D Adaptive filtering method (called Signal Subspace Processing, SSP) compensates for
 - 1. Unknown variations of the electronics, antennas, etc. of the two SAR databases
 - 2. Spatial warping in the test and reference imagery due to unknown INS errors and/or unknown variations in target area height
- Interferometric (phase only) processing for change detection could also benefit from adaptively calibrated imagery







 A realistic miscalibration model for the two receiver channels is based on the fact that the <u>filter is spatially-varying</u>. In this case, the relationship between the test and reference images can be expressed via the following:

$$\hat{f}_{RT}(x,y) = \int f_R(x-u,y-v) h_{xy}(u,v) du dv$$

where in this model the filter $h_{xy}(u,v)$ varies with the spatial coordinates (x, y).





- While the above model is a more suitable one, however, it is computationally prohibitive to implement the LMS or SSP method for this scenario.
- A practical alternative is to assume that the filter is approximately spatially-invariant within a small area in the spatial domain.
- In this case, we can divide the imaging scene into subpatches within which the filter can be approximated to be spatially-invariant.







LSSP







 After the calibration filter is estimated for each subpatch, an approach that we call *Global Signal Subspace Processing* (GSSP) is used to estimate the original spatially-varying filter





- Available samples of 2D adaptive filter for the subpatches $h_{\ell}(u,v)$ are at the grid point (x_{ℓ}, y_{ℓ}) ; these are shown as blue dots.
- For every (u,v) (that is the 2D filter domain), the values of the 2D spatiallyvarying filter $h_{xv}(u,v)$ are interpolated on the original image grid in the spatial domain (x, y) (black dots) from the available filter samples $h_{\ell}(u,v)$ at the grid points (x_{ℓ}, y_{ℓ}) (blue dots).



GSSP



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2.3 SAR-MTI Using Monostatic and Along-Track Bistatic Monopulse Configuration (DPCA-MTI, Option 1)

maging System Geometry: Top View







Coherent Clutter Suppression Using GSSP on Slant-Plane













Results with Gotcha SAR Data

Subaperture Processing: 1024 PRIs (.5 sec) per Subaperture 512-PRI Overlapping Subapertures (.25 sec updating)



Imaging System Geometry: Subapertures 1-40







Full-Aperture Reconstruction







Subaperture Reconstruction





UTM Reconstruction: FP-128; Subaperture 1



MTI Detections: Coherent Single Pass Dual Receivers







3. Multiple Moving Targets Association and Tracking



- An algorithm that uses linear prediction to associate MTI hits in IR and visible camera imagery is the basis of our approach for SAR-MTI tracking problem
- This approach is used on processing the MTI hits on the ground plane SAR image
- The algorithm could exploit our analytical study of SAR geolocation based on radialrange and angular-Doppler shift information of MTI hits (that is discussed later)





Ground Plane







• Moving target coordinates at zero slowtime $\tau = 0$ of a subaperture:

$$\left(X_{ ext{target}}^{(\ell)}, Y_{ ext{target}}^{(\ell)}, Z_{ ext{target}}^{(\ell)}\right)$$

 3D velocity of moving target (is assumed to be a constant within a subaperture but may vary from one subaperture to another):

$$\left(v_{x ext{target}}^{(\ell)}, v_{y ext{target}}^{(\ell)}, v_{z ext{target}}^{(\ell)}\right)$$





 Distance of moving target from radar (<u>radial-range</u>) as a function of slow-time:

$$R_{\text{radar - target}}^{(\ell)} \left(\tau\right) = \begin{bmatrix} \left(X_{\text{radar}}^{(\ell)} + v_{x\text{radar}}^{(\ell)} \tau - X_{\text{target}}^{(\ell)} - v_{x\text{target}}^{(\ell)} \tau\right)^{2} + \\ \left(Y_{\text{radar}}^{(\ell)} + v_{y\text{radar}}^{(\ell)} \tau - Y_{\text{target}}^{(\ell)} - v_{y\text{target}}^{(\ell)} \tau\right)^{2} + \\ \left(Z_{\text{radar}}^{(\ell)} + v_{z\text{radar}}^{(\ell)} \tau - Z_{\text{target}}^{(\ell)} - v_{z\text{target}}^{(\ell)} \tau\right)^{2} \end{bmatrix}^{1/2}$$

• <u>Angular Doppler frequency</u> of moving target as a function of slow-time:





where

$$sin \phi_{radar-target}^{(\ell)}(\tau) = \frac{\frac{d}{d\tau} R_{radar-target}^{(\ell)}(\tau)}{v_{radar}^{(\ell)}}$$

$$= \frac{\left[\begin{pmatrix} v_{xradar}^{(\ell)} - v_{xtarget}^{(\ell)} \end{pmatrix} \begin{pmatrix} X_{radar}^{(\ell)} + v_{xradar}^{(\ell)} \tau - X_{target}^{(\ell)} - v_{xtarget}^{(\ell)} \tau \end{pmatrix} + \\ \begin{pmatrix} v_{radar}^{(\ell)} - v_{ytarget}^{(\ell)} \end{pmatrix} \begin{pmatrix} Y_{radar}^{(\ell)} + v_{yradar}^{(\ell)} \tau - Y_{target}^{(\ell)} - v_{ytarget}^{(\ell)} \tau \end{pmatrix} + \\ \begin{pmatrix} v_{radar}^{(\ell)} - v_{ytarget}^{(\ell)} \end{pmatrix} \begin{pmatrix} Y_{radar}^{(\ell)} + v_{yradar}^{(\ell)} \tau - Y_{target}^{(\ell)} - v_{ytarget}^{(\ell)} \tau \end{pmatrix} + \\ \begin{pmatrix} v_{radar}^{(\ell)} - v_{ztarget}^{(\ell)} \end{pmatrix} \begin{pmatrix} Z_{radar}^{(\ell)} + v_{zradar}^{(\ell)} \tau - Z_{target}^{(\ell)} - v_{ztarget}^{(\ell)} \tau \end{pmatrix} + \\ \begin{pmatrix} v_{radar}^{(\ell)} - v_{ztarget}^{(\ell)} \end{pmatrix} \begin{pmatrix} Z_{radar}^{(\ell)} + v_{zradar}^{(\ell)} \tau - Z_{target}^{(\ell)} - v_{ztarget}^{(\ell)} \tau \end{pmatrix} + \\ \end{pmatrix} + \\ \frac{v_{radar}^{(\ell)} R_{radar}^{(\ell)} \tau - Z_{target}^{(\ell)} - v_{ztarget}^{(\ell)} \tau }{v_{ztarget}^{(\ell)} - v_{ztarget}^{(\ell)} \tau } + v_{zradar}^{(\ell)} \tau - Z_{target}^{(\ell)} - v_{ztarget}^{(\ell)} \tau \end{pmatrix} + \\ \frac{v_{radar}^{(\ell)} R_{radar}^{(\ell)} \tau - Z_{target}^{(\ell)} \tau }{v_{radar}^{(\ell)} - v_{ztarget}^{(\ell)} \tau } + v_{zradar}^{(\ell)} \tau - Z_{target}^{(\ell)} \tau \end{pmatrix} + \\ \frac{v_{radar}^{(\ell)} R_{radar}^{(\ell)} \tau - V_{ztarget}^{(\ell)} \tau }{v_{radar}^{(\ell)} - v_{ztarget}^{(\ell)} \tau } + v_{zradar}^{(\ell)} \tau - Z_{target}^{(\ell)} \tau } + v_{zradar}^{(\ell)} \tau - Z_{target}^{(\ell)} \tau + v_{zradar}^{(\ell)} \tau +$$







- Radial-ranges of a moving target for the subapertures could be mapped into the network of roads on the ground plane
- Operator/computer could determine which road is the logical/correct choice by:
 - a. Estimating target velocity on a road
 - b. Calculating subaperture angular Doppler values from the estimated velocity and other available radar/target parameters
 - c. Comparing calculated and actual angular Doppler data













MTI Detections for an Acutal Moving Target

MTI detections for an actual moving target in subapertures 1-40 (red circles), and the lines of constant radial range for the moving target for each subaperture (blue lines)





MTI Results Validation and Target Geolocation via Measured SAR Data & Simulation



MTI Detections & Road Mapping for Simulated Target 400 300 200 **MTI Hits** Northing, m 100 Simulated **Motion Path On J Street** -100 -200 · -300 -200 -100 0 100 200 300 Easting, m

MTI detections for the first simulated moving target (on J Street with speed of 16 mph) in subapertures 1-40 (red circles), the lines of constant radial range for the moving target for each subaperture (blue lines), and the road mapping of the target on J Street (red stars)

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MTI detections for the second simulated moving target (on P Street with speed of 24 mph) in subapertures 1-40 (red circles), the lines of constant radial range for the moving target for each subaperture (blue lines), and the road mapping of the target on P Street (red stars)





Target on **P** Street moving at 24 mph fits the model

MTI detections for an actual moving target

Easting, m







We Presented:

- 1. Algorithm to detect multiple moving targets from along-track monopulse SAR data; the algorithm blindly calibrates for various system errors in the two monopulse channels that vary in the image spatial domain.
- 2. Association, tracking and geolocation algorithms that depend on the signal properties of a moving target SAR signature and the network of roads in the interrogated scene.

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